**PERTH MODERN SCHOOL**



**YR11 MATHEMATICS SPECIALIST – 2019**

**TEST 1 – Reasoning & Permutations**

**NAME: \_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_ DATE:\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_**

**Teacher’s Name\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_**

To achieve full marks working and reasoning should be shown.

**This is a *Calculator Assumed Assessment – 45 minutes / 38 marks***

**You may have notes on one side of an A4 sheet of paper.**

This section has been intentionally left blank

1. **[ 3 marks]**
2. Suppose a mathematical statement of the form is true. Then (Circle your answer)
3. Its converse will always be true.
4. Its converse will always be false.
5. Its negation will be always be true.
6. Its contrapositive will always be true.
7. Its contrapositive will always be false.
8. Suppose *n* is an integer. Consider the statement: If *n2* is even then *n* is even.

The converse of this statement is: (Circle your answer)

1. If *n*2 is odd, then *n* is even.

1. If *n*2 is even, then *n* is odd.
2. If *n*2 is odd, then *n* is odd.

(d) If *n* is odd, then *n*2 is odd.

1. If *n* is even, then *n*2 is even.
2. Consider the statement: The number is a composite number for every positive integer *n*.

The negation of this statement is: (Circle your answer)

1. The number is a prime number for some prime number *n*.
2. The number is a prime number for every prime number *n*.
3. The number is a prime number for every positive integer *n*.
4. The number is a prime number for some positive integer *n*.

(e) The number is a composite number for some positive integer *n*.

2. **[6 marks]**

Use mathematical induction to prove that is divisible by 12 for all integers n > 1.

3. **[8 marks]**

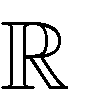
For , let

Use mathematical induction to prove that, for all integers with ,

4. **[6 marks]**

Use the fact that if is divisible by 3, then n is divisible by 3 to prove that is irrational.

5. **[5 marks]**

Suppose that *a*, *b*  and consider the statement: If *ab* is irrational then either *a* or *b* is irrational.

1. Write down the contrapositive of this statement.
2. Prove the contrapositive of this statement.

6. **[5 marks]**

From the letters of the word **FACTORISE**, words of 5 letters are arranged without repeating letters.

How many of these arrangements of 5 letters:-

(a) are possible altogether

(b) begin with the letters **AR** in that particular order

(c) end with the letter **T**

1. start with **AR** in any order (ie **AR** or **RA**) and end with **T**

7. **[5 marks]**

Using the digits from this list: 0, 3, 4, 5, 6, 8 determine:

a) How many 4 digit numbers can be made that are greater than 4000?

(No repetition allowed. You cannot start the number with zero)

b) How many 4 digit numbers are even and greater than 4000?

(No repetition allowed. You cannot start the number with zero)

**This page has been left blank intentionally.**